

Data Structures thus far:

- array { own & STL
vector < >
- linked list { own & STL
list < >
- stack (queue)
- bin heap
- binary search tree (BST)
- AVL tree (balanced BST)
- hash table
- associative array (STL
map < >)
- Kt-tree

- matrix:

$$\begin{bmatrix} a_{ij} & \dots & \dots \\ \vdots & \ddots & \ddots \end{bmatrix} \begin{matrix} \text{rows} \\ \text{cols} \end{matrix}$$

- particularly useful for
3D rotations (in
computer graphics)

↳ 4x4 matrix

e.g. 3D point (y. vert. x)

$$\begin{bmatrix} x & y & z & 1 \end{bmatrix} \begin{bmatrix} \cos\theta & \sin\theta & 0 & 0 \\ -\sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

1×4

4×4

$$= \begin{bmatrix} x' & y' & z' & 1 \end{bmatrix}$$

1×4

rotates point
about z-axis by θ°

Not by y :

$$\left[\begin{array}{cccc|c} \cos\theta & 0 & \sin\theta & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{array} \right]$$

Similarly for
not by x

4x4
matrix

$[x \ y \ z \ 1]$: 4-vector
a 'one', representing
(3D)

point using

homogeneous words

- matrix in C++?

- use private:

```
std::vector<std::vector<T>>
```

```
    all;
```

Vector of vectors

for any $m \times n$ matrix

- Constructor 1

Matrix (int r = 4, int c = 4):

arr(r)

} for (int i = 0; i < r; i++)
arr[i].resize(c); }

- accessor/mutator operators

```
const std::vector<T>&  
operator[](int v) const  
{ return arr[v]; }
```

```
std::vector<T>&  
operator()(int v)  
{ return arr[v]; }
```


- other functions:

e.g. operator - (void)

operator! (void)

Unary
operator,

negating each
cell

Matrix
inverse

e.g. A ,

A^{-1} is inverse of A

$$AA^{-1} = I$$

e.g., operator! (void):

// compute matrix inverse

e.g., look up "Num.

recipes in C"

(or C++) & the

something like LU

decomposition

- idea for math lib
($\hat{=}$ code development
in general) :

Implement desired
functionality $\hat{=}$ write
test suite to validate
code
↳ test driver.